



**HAT**  
**Advanced Logarithmic Thinking!**

**12/4/17**

Warm Up: Solve

$$1) \log_3 x + \log_3 (x-8) = 2$$

$$\log_3 (x^2 - 8x) = 3^2$$

$$x^2 - 8x = 9$$

$$x^2 - 8x - 9 = 0 \quad (x-9)(x+1) = 0$$

$$\boxed{x=9}$$
~~$$x=-1$$~~

$$2) \frac{3 \log_4 6x}{3} = \frac{9}{3}$$

$${}_4 \log_4 6x = \frac{9}{3}$$

$${}_6 4 = 6x$$

$$\boxed{x = 10 \frac{2}{3}}$$

Which student solved for  $x$  correctly in the following problem?  $2 \log x = 4$

Alice

$$2 \log x = 4$$

$$\log x^2 = 4$$

$$x^2 = 4$$

$$x = 2$$

Bob

$$2 \log x = 4$$

$$\log x^2 = 4$$

$$x^2 = 4$$

$$x = \pm 2$$

Carl

$$2 \log x = 4$$

$$\log x^2 = 4$$

$$x^2 = 10^4$$

$$x^2 = 10000$$

$$x = 100$$

David

$$2 \log x = 4$$

$$\log x^2 = 4$$

$$x^2 = 10^4$$

$$x^2 = 10000$$

$$x = \times 100$$

Which student solved for  $x$  correctly in the following problem?  $2 \log 3 + \log x = \log 36$

Astro

$$2 \log 3 + \log x = \log 36$$

$$\log 9 + \log x = \log 36$$

$$\log 9x = \log 36$$

$$9x = 36$$

$$x = 4$$

Chu

$$2 \log 3 + \log x = \log 36$$

$$2(\log 3 + \log x) = \log 36$$

$$2 \log 3x = \log 36$$

$$\log 3x^2 = \log 36$$

$$3x^2 = 36$$

$$x^2 = 12$$

$$x = \sqrt{12}$$

Bella

$$2 \log 3 + \log x = \log 36$$

$$\log 9 + \log x = \log 36$$

$$\log (9 + x) = \log 36$$

$$9 + x = 36$$

$$x = 27$$

Domingo

$$2 \log 3 + \log x = \log 36$$

$$2(\log 3 + \log x) = \log 36$$

$$2 \log 3x = \log 36$$

$$\log (3x)^2 = \log 36$$

$$9x^2 = 36$$

$$x^2 = 4$$

$$x = 2$$

Ex#1: Solve  $4^{2x} - 7 \cdot 4^x + 12 = 0$

$$w = 4^x \quad (4^x)^2 \quad 4^{2x} - 7 \cdot 4^x = -12$$

$$4 = 4^x \quad w^2 - 7w + 12 = 0$$

$$x = 1$$

$$(w-4)(w-3)$$

$$3 = 4^x$$

$\log_4 3 = \log_4 4^x$

$$w = 4 \quad w = 3$$

$$x = 0.792x$$