

$$\log_3 27$$

3



$$\log_2 64$$

6



$$\log_{\frac{1}{8}} \frac{1}{512}$$

3



$$\log_7 \frac{1}{7}$$

-1



$$\log_{\frac{1}{3}} 81$$

-4



$$\log_4 (-16)$$

undefined

$$\log_5 1$$

0



$$\log_{\frac{1}{10}} 100$$

-2



$$\log_4 8$$

 $\frac{3}{2}$ 

$$\log_2 1$$

0



$$\log_4 32$$

 $\frac{5}{2}$ 

$$\log_2 0$$

undefined



Warm Up: Use INVERSES to find the value of  $x$ .

a)  $\log_3 x = 2$

$x = 9$  NC

b)  $3^x = 9 \rightarrow \log_3 3^x = \log_3 9$  NC  
 $x = 2$

c)  $3^x = 8$

d)  $2.4^x = 7.2$

e)  $3 \cdot 2^x = 48$

f)  $4.1 \cdot 2.6^x = 32.8$

$\frac{3 \cdot 2^x = 48}{3} \quad \frac{48}{3}$   
 NC  
 $2^x = 16$   
 $\log_2 2^x = \log_2 16$   
 $x = 4$

$\frac{4.1 \cdot 2.6^x = 32.8}{4.1} \quad \frac{32.8}{4.1}$   
 $2.6^x = 8$  Calc  
 $\log_{2.6} 2.6^x = \log_{2.6} 8$   
 $x = \log_{2.6} 8$   
 $x \approx 2.176$

$\log_{2.4} 2.4^x = \log_{2.4} (7.2)$

$x = \log_{2.4} (7.2)$   
 $x \approx 2.255$   
 Calc

$\log_3 3^x = \log_3 8$   
 $x = \log_3 8$   
 $x \approx 1.893$   
 Calc

Solve.

$$4^{10} + 4^{10} = 8^x$$

$$x=7$$

$$2 \cdot 4^{10} = 8^x$$

$$2 \cdot 2^{20} = 2^{3x}$$

$$2^{21} = 2^{3x}$$

$$21 = 3x$$

$$x=7$$

$$16 \cdot 2^{2x-4} = \frac{8}{2^{x-6}}$$

$$x=3$$

$$2^4 \cdot 2^{2x-4} = \frac{2^3}{2^{x-6}}$$

$$2^{2x} = 2^{3-(x-6)}$$

$$2x = 3 - x + 6$$

$$+x \quad +x$$

$$3x = 9$$

$$x=3$$

Simplify.

$$\log_{36}(\log_2 64)$$

$$\log_{36}(6)$$

$$\log_{36}(36^{1/2}) = \boxed{\frac{1}{2}}$$

Solve.

$$\log_7 \sqrt[3]{49} \cdot 10^{\log_{10} \left(\frac{1}{9}\right)^{-1/2}} = 4^{\log_4 x}$$

$$\log_7 7^{2/3} \cdot \left(\frac{1}{9}\right)^{-1/2} = x$$

$$x = 2$$

$$\frac{2}{3} \cdot 3 = x$$

If  $f(x) = 15 \cdot 3^{x-6} - 2$

find:  $n = f^{-1}(133)$

$$x = 15 \cdot 3^{y-6} - 2$$

$$\frac{x+2}{15} = \frac{15 \cdot 3^{y-6}}{15}$$

$$\log_3 \frac{x+2}{15} = \log_3 3^{y-6}$$

$$\log_3 \left( \frac{x+2}{15} \right) = y-6$$

$$\log_3 \left( \frac{x+2}{15} \right) + 6 = y$$

$$f^{-1}(x) = \log_3 \left( \frac{x+2}{15} \right) + 6$$

$$f^{-1}(133) = \log_3 \left( \frac{135}{15} \right) + 6$$

$$f^{-1}(133) = \log_3 9 + 6$$

$$f^{-1}(133) = 8$$

$$\log_4(x+2) \leq 1$$

$$\log_{\frac{1}{2}} x \geq 2$$

$$\log_{\frac{1}{3}}(3x-4) \geq -3$$