

HAT

Inverse Relations and Functions

10/27/17

What are examples of inverse operations?

powers
& roots

addition & subtraction

mult &
division

EX #1: Given $y = x + 3$, find the inverse equation?

$$y = x - 3$$

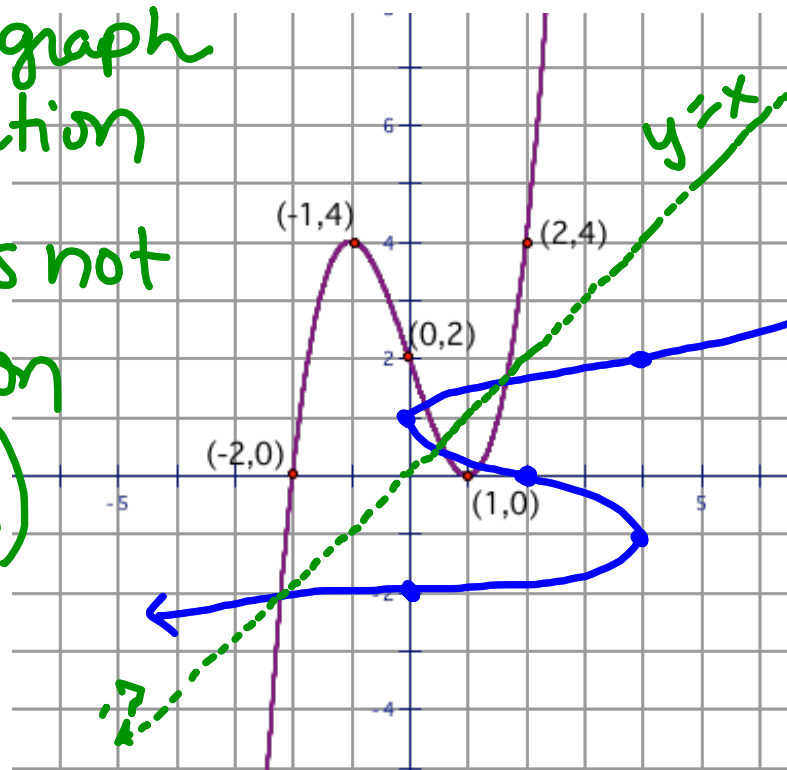
EX #2: Find the inverse equation of $y = \frac{x}{5}$

$$y = 5x$$

EX #3: Graph the inverse. Interchange x & y values

Original graph
is a function

Inverse is not
a function
(Relation)



Graph
of
the
inverse

Is the original graph a function?

Yes

Is the inverse graph a function?

NO

If the original function passes the horizontal line test, then the inverse is a function

(passes VLT)

Functions that pass the horiz. line test are called one to one

functions. Exactly 1 x value for each y value.

EX #4:

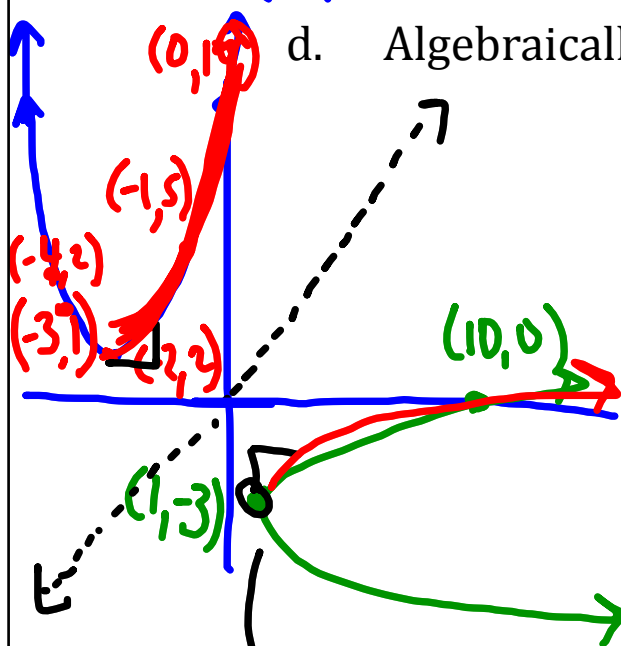
a. Graph $f(x) = (x+3)^2 + 1, x \geq -3$

b. Graph $f^{-1}(x)$ ← The inverse function

c. Write the equation of $f^{-1}(x)$

d. Algebraically determine the equation of $f^{-1}(x)$

Restrict the domain



$$f^{-1}(x) = \sqrt{x-1} - 3$$

$y = -\sqrt{x-1} - 3$ ← relation

EX #5: Using the equations from Ex#4...

Find $(f \circ f^{-1})(x)$ and $(f^{-1} \circ f)(x)$

Assignment:

page 396 #18, 22, 25, 26, 32, 35, 36, 49, 53, 56